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Influence of a magnetic guide field on wakefield acceleration

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Enhancement of the trapping and optimization of the beam quality are two key issues of Laser Wake Field Acceleration (LWFA). The influence of stochastic acceleration on the trapping of electrons is compared to the one of cold injection. It is shown that when considering a high intensity wave perturbed by a low intensity counter-propagating wave, in the non-linear blowout regime, the influence of the colliding pulses polarizations (either parallel linear or positive circular) on the beam quality seems weak when the electron density is below $\sim 10^{-3}$ critical density. The effect of a homogenous constant magnetic field B_0 , parallel to the direction of propagation of the pump pulse, is studied in the blowout regime. Transverse currents are generated at the rim of the bubble, which results in the amplification of the B_0 field at the rear of the bubble. Without B_0 field the beam periodically explodes and re-confines, this phenomenon is suppressed when B_0 reaches some threshold, which is a function of the laser pulses parameters (intensity, waist, duration). Therefore the dynamics of the beam is modified, its maximum energy is slightly boosted and above all transverse emittance reduced. Moreover the low energy tail, observed in the non magnetized case, can be completely suppressed leading to very sharp mono-energetic beam when B_0 is applied. If the available B_0 field is limited then one has to fine-tune the spatio-temporal shape and intensity of the colliding pulse in order to get an acute control on the beam quality.

I. INTRODUCTION

In laser-wakefield acceleration (LWFA) [1–4], a laser creates a plasma wave wakefield with a phase velocity close to the speed of light (c). The acceleration gradients in these wakefields can easily exceed 100 GeV/m, hence a cm-long plasma based accelerator can produce GeV-energy electron beams. A particle injected in such a wave gains energy from the longitudinal component of the electric field, as long as the pump pulse is not depleted and the dephasing length is not reached. These wakefields have ideal properties for accelerating electrons. The transverse focusing field increases linearly with the radial distance and the accelerating longitudinal field is independent of the radial coordinate [5, 6]. LWFA can be split into three different options. The first corresponds to a plasma density $n_e \approx 10^{19} \text{cm}^{-3}$, a pulse length ($c\tau$) matching half of a plasma period and a spot size (w_0) roughly equals to the bubble radius, $w_0 \approx c\tau \approx \sqrt{a_0}$, where a_0 is the normalized vector potential of the laser. This is the idea of the bubble regime [7, 8]. For these conditions, a hundred-joule class laser would have an intensity of the order $\sim 10^{21} \text{W cm}^{-2}$. In this regime, the electrons are continuously injected, this results in tremendous beam loading and the loaded wake is noisy. In this paper we explore different techniques to improve the beam quality of LWFA when electrons are injected in the wake with a colliding pulse. Hence, the bubble regime is not appropriate. We rather select moderate laser intensity $I \leq 10^{19} \text{W.cm}^{-2}$ and plasma density $n_e \leq 10^{18} \text{cm}^{-3}$ according to the guidelines proposed

by Lu et al.[9] to achieve a more controlled and stable blowout of the electrons. Self-injection of electrons can occur when the pump pulse intensity is high but the accelerating structure is almost the same. In this frame beam loading effects clamp further injection leading to beams with a smaller energy spread. In order to limit the computational requirements of our PIC simulations the propagation of the pump pulse will not exceed 1 cm. We tend to avoid self-injection into the wake by adjusting the pump pulse intensity and the electronic density. Many different combinations of polarizations can be chosen for both waves, each of these possibilities results in particular force acting on the plasma electrons, when the two waves collide [10]. The first point of this article is to summarize the dependance to pump and colliding pulse intensities, and to plasma density of this force. The relative influence of stochastic heating and beat wave force on the injection mechanism, and later on the beam quality will be discussed. After the choice of polarization in the blowout regime is clarified, we focus on the study of wakefield acceleration in the presence of an external, homogenous, magnetic field and study its influence through simulations. The mechanisms leading to the enhancement of the beam quality will be examined. In a third part, fine-tuning of the counter-propagating low intensity pulse will be considered in order to limit the intensity of the external field. This situation will be illustrated in the case when the intensity of the pump pulse is raised to $a_0 = 10$. Then we will conclude.

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II. SENSITIVITY OF BEAM INJECTION TO WAVE INTENSITY, PLASMA DENSITY AND POLARISATION OF LASERS

A. Basic principles

The wakefield propagates in the plasma at the group velocity of the laser β_g defined by : $\beta_g = v_g/c = \left(1 - \frac{\omega_p^2}{\omega_0^2}\right)^{1/2}$, where c is the speed of light, ω_p and ω_0 respectively denote the plasma and laser frequencies. We use the quasi-static approximation and assume that the potential ϕ created by the pump pulse only depends on $\xi = x - \beta_g t$, where x and t denote the space and time coordinates normalized by c/ω_0 and ω_0^{-1} respectively. Then, the hamiltonian of an electron in the wakefield potential ϕ , created by the pump pulse, reads :

$$H(\xi, p_x) = \sqrt{\gamma_\perp^2 + p_x^2} - \beta_g p_x - \phi(\xi), \quad (1)$$

where $\gamma_\perp^2 = 1 + \mathbf{p}_\perp^2$. The normalized transverse momentum is defined by $\mathbf{p}_\perp = \frac{\mathbf{u}_\perp}{m_e c}$, where \mathbf{u}_\perp is the transverse momentum and m_e denotes the electron mass. The hamiltonian of a particle is an invariant $H(\xi, p_x) = H_0$, using (1) we deduce two solutions for the longitudinal momentum :

$$p_x^\pm(\xi) = \beta_g \gamma_g^2 (H_0 + \phi) \pm \gamma_g (\gamma_g^2 (H_0 + \phi)^2 - \gamma_\perp^2)^{1/2}, \quad (2)$$

where $\gamma_g^2 = 1 + \beta_g^2$. The separatrix between trapped and untrapped orbits is given by a critical value, $H_s = \frac{\gamma_\perp}{\gamma_g} - \phi_{\min}$, of the Hamiltonian. Replacing H_0 by H_s in (2) and retaining p_x^\pm we get the two branches of $p_x^{\text{sep}}(\xi)$.

Let us now comment the dynamics of an electron in vacuum, in the presence of two counter-propagating laser pulses. The hamiltonian reads $H(u_x, x) = (1 + u_x^2 + u_\perp^2)^{1/2} = \gamma$, the longitudinal force acting on the electron is given by

$$\frac{du_x}{dt} = -\frac{\partial H}{\partial x} = -\frac{1}{2\gamma} \frac{\partial u_\perp^2}{\partial x}. \quad (3)$$

Taking only into account the influence of the lasers, denoted by their potential vectors \mathbf{A}_0 and \mathbf{A}_1 , we have $\mathbf{u}_\perp = \mathbf{A}_0 + \mathbf{A}_1$. We will consider parallel linear polarization (P linear polarization) and positive circular polarization, that is $\mathbf{u}_\perp = a_0 \cos(\omega_0 t - k_0 x) \mathbf{e}_y + a_1 \cos(\omega_0 t + k_0 x) \mathbf{e}_y$ and $\mathbf{u}_\perp = \left[\frac{a_0}{\sqrt{2}} \cos(\omega_0 t - k_0 x) + \frac{a_1}{\sqrt{2}} \cos(\omega_0 t + k_0 x) \right] \mathbf{e}_y + \left[\frac{a_0}{\sqrt{2}} \sin(\omega_0 t - k_0 x) + \frac{a_1}{\sqrt{2}} \sin(\omega_0 t + k_0 x) \right] \mathbf{e}_z$ respectively. Substituting the above expressions in Eq. (3) yields

$$F_x = \frac{-1}{2\gamma} [a_0^2 k_0 \sin(2(\omega_0 t - k_0 x)) - a_1^2 k_0 \sin(2(\omega_0 t + k_0 x))] + \frac{k_0 a_0 a_1}{\gamma} \sin(2k_0 x), \quad (4)$$

for the P linear polarization case, and

$$F_x = \frac{k_0 a_0 a_1}{\gamma} \sin(2k_0 x) \equiv F_{bw}, \quad (5)$$

for the positive circular polarization case. When P linear or positive circular polarizations are used Eqs. (4) and (5) show the existence of a force F_{bw} spatially oscillating with a $\lambda_0/2$ period. This force is not time-dependant, it is usually interpreted as a ponderomotive force associated with the beat-wave [10–13]. We should compare the beatwave force F_{bw} to the longitudinal ponderomotive force, this latter scales as $F_p = (2\gamma)^{-1} a_0^2 / (c\tau)$ where τ is the pulse duration. Taking the maximum value of F_{bw} the ratio F_{bw}/F_p becomes

$$F_{bw}/F_p = 2a_1 \omega_0 \tau / a_0. \quad (6)$$

When $F_{bw}/F_p > 1$ electrons are trapped inside the $\lambda_0/2$ -long beatwave buckets and cannot be wiped out by the longitudinal ponderomotive force. On the whole for both polarizations electrons will undergo the beatwave force, therefore when the separatrix is such that $\min(u_x) < 0$ electrons will be trapped in the wakefield as a bunch [14]. However in the P linear polarization case other terms are added to the force and the equations of the motion are no longer integrable, electron trajectories become chaotic [15]. This phenomenon known as stochastic heating can provide very large momenta to some electrons [16–22]. When $\min(u_x) \geq 0$ the beatwave force is not efficient and electrons can hardly be trapped with positive circular polarizations. In this case P linearly polarized colliding waves are necessary to give electrons the appropriate momentum in order to fill the gap between trapped and untrapped orbits. In the following two subsections, the sensibility of the injection process to polarization and intensity of the waves will be summarized.

B. Low density: Strong dependance to polarization and wave intensity

When the plasma density is about $\sim 10^{-3} n_c$ a weak variation of the pump pulse is sufficient to modify the mechanisms allowing trapping of a bucket in the wakefield. To illustrate this strong dependance to laser parameters we launched three sets of simulations with the PIC code CALDER [23]. The simulation setup consists in two 30 fs linearly polarized waves with wavelength $\lambda = 0.8 \mu\text{m}$ having their electric fields either linearly or circularly polarized (orthogonal linear polarization is denoted by S). The pump pulse, which creates the accelerating wakefield, is focused to an $18 \mu\text{m}$ full width at half maximum (fwhm). The peak normalized vector potential of the main pulse is associated to the laser intensity I by the formula $a = 0.853 \times 10^{-9} \lambda(\mu\text{m}) [I(\text{W cm}^{-2})]^{1/2}$, we considered $a = 1.5$ and $a = 2$. The low intensity pulse is counter-propagating and is focused to a $31 \mu\text{m}$ focal spot at a peak normalized vector potential $a_1 = 0.1$ or

0.4. The waves interact with a mm-size plasma with a density $n_e = 4.3 \times 10^{-3} n_c$. The fluctuations between the two regimes are illustrated by Figs. 1. When $a = 1.5$ and $a_1 = 0.4$ the 1D separatrix between trapped and opened orbits is higher than $p_x = 0$, in this case the beatwave force cannot provide enough momentum to electrons to push them in the wakefield. Nevertheless stochastic heating due to P linear polarizations is a way to bridge the gap and inject a bunch in the wakefield (Fig. 1(a)). When $a = 2$ the 1D separatrix is lowered ($\min(p_x) < 0$), in this case the beatwave force is enough to trap electrons in the wake therefore we can accelerate a beam using either P linear or positive circular polarizations. Note that no trapping occurs with negative circular polarizations, which is consistent with the theory introduced in subsection II A. Indeed straightforward algebra gives $F_x = 0$, then the ponderomotive force hinders trapping of electrons. The quality of the accelerated beam will depend on the force which dominates during collision of the pulses. A relatively high intensity of the counter propagating laser ($a_1 = 0.4$) will foster stochastic heating [21, 22] and a higher charge will be injected with P linear polarizations compared to positive circular polarizations (Fig. 1(b)). On the contrary, if we reduce the intensity of the counter propagating pulse ($a_1 = 0.1$) the beatwave force is favored and rules the injection mechanism (Fig. 1(c)). In this latter case, the beam quality is better without stochastic heating.

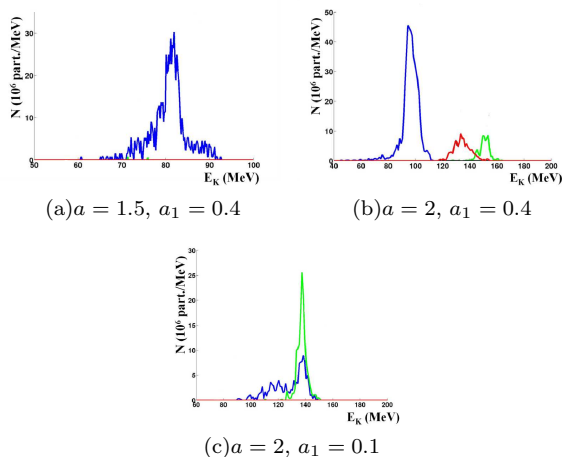


FIG. 1: Electron energy distribution obtained long after the collision of the two waves with $n_e = 4.3 \times 10^{-3} n_c$. P linear polarizations (blue curve). Positive circular polarizations (green curve). S linear polarizations (red curve) and negative circular polarizations (black curve, overlaid with axis in this case).

C. Very low density: Weak dependance to laser polarization

We now chose parameters relevant for the study of the blowout regime [6, 24–26]. The plasma density was set to $n_e = 2.5 \times 10^{-4} n_c$ and the pump pulse intensity to $a = 4$, the rest of the simulation setup was not modified. Considering two circularly polarized waves rotating in the same direction (positive circular polarizations) is as efficient as considering P linear polarizations (Fig. 2). It means that in this case cold injection [14, 27] due to the beating force is the key mechanism governing electron injection. Stochastic acceleration weakly changes the number and the energy of electrons trapped in the wake field. The electron momentum distribution along the direction of propagation of the waves during their collision shows that the effects on electron dynamics of the two polarizations are close, as a result the electron energy distributions are almost identical (Fig. 2). This

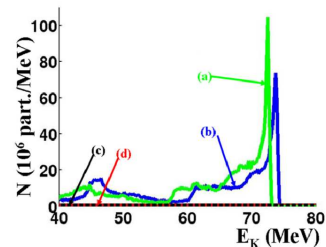


FIG. 2: Electron energy distribution from 2D PIC simulations. $a = 4$, $a_1 = 0.1$ and $n_e = 2.5 \times 10^{-4} n_c$. (a): Positive circular polarizations. (b): P linear polarizations. (c): Negative circular polarizations. (d): S linear polarizations.

dominant influence of the beating force upon injection was not clearly stated by Davoine *et al.* [14], here we underline that no relevant difference is triggered through use of P linear polarizations or positive circular polarizations in the blowout regime. The next section is devoted to the study of a new means to enhance beam quality after colliding pulse injection, in the blowout regime.

III. INFLUENCE OF A MAGNETIC GUIDE FIELD

The influence of a constant homogeneous guide magnetic field on LWFA is studied in this part. This magnetic field is assumed to be parallel to the direction of propagation of the waves. Electrons are still externally injected using a colliding counter propagating laser pulse [13]. The idea is to guide the electrons in order to improve the quality of the beam which is trapped in the wake field. This mechanism was first proposed in the context of LWFA, with a single pump laser ($a = 3.5$) and an electronic density $n_e = 3 \times 10^{-3} n_c$ prone to self-injection into the wake field [28], with these parameters

self-injection can be dramatically enhanced and beam quality degraded. Here we aim at studying the influence of a magnetic guide field in the blowout regime [9] with colliding pulse injection of the electrons, hence we chose $a = 4$ and $n_e = 4.4 \times 10^{17} \text{cm}^{-3} = 2.5 \times 10^{-4} n_c$, thus abiding by $a_0 \geq 4$ and $2 \leq a_0 \leq 2\omega_0/\omega_p$ criteria proposed by Martins *et al.* [25]. The required magnetic field necessary to curve electron trajectories is about a hundred teslas [28], such values are particularly strong but still available from the current pulsed magnet technology [29], the most advanced magnets can reach 90T for tens of ms durations and centimeter size lengths [30]. The simulation setup consists in two 30 fs linearly polarized counterpropagating waves with $\lambda = 0.8 \mu\text{m}$ wavelength. They propagate along a constant homogeneous guide field B_0 in a cm-long plasma, the normalised value of B_0 is given by $\widetilde{B}_0 = eB_0/(m_e\omega_0)$. Their electric fields are in the same plane (P linear polarizations). The pump pulse, which creates the accelerating wakefield, is focused to an $18 \mu\text{m}$ full width at half maximum. The peak normalized vector potential for this pulse is still $a = 4$. The low intensity pulse is focused to a $31 \mu\text{m}$ focal spot at a peak normalized vector potential $a_1 = 0.1$. The plasma frequency in the presence of a magnetic field can be approximated by $\omega_m = (\omega_e^2 + \Omega^2)^{1/2}$ where ω_m and ω_e represent the frequencies of the magnetized and unmagnetized plasma, respectively. The cyclotron frequency is defined by $\Omega = eB_0/m$. When $B_0 = 125 \text{T}$ and $B_0 = 250 \text{T}$, one has $\Omega^2/\omega_e^2 = 0.34$ and $\Omega^2/\omega_e^2 = 1.38$ respectively which proves that the magnetization of the plasma may have some effect on the deformation of the wakefield as will be further discussed. Before the collision of the waves the magnetization has no influence on self-injection, no electron is trapped in the wake.

A. Electronic density and transverse currents induced at the rim of the bubble

Let us first identify the differences brought by the addition of a magnetic guide field to the electronic distribution at the vicinity of the bubble boundaries (Figs. 3). After the electron beam injection into the wake field, the strong ponderomotive force due to the main pulse still repels electrons and thus provides them longitudinal and transverse momenta. In the absence of magnetic field, electrons are submitted to the recall electric field induced by the bubble but the balance between this force and the ponderomotive force is favorable to the latter ; as a result electrons flee along straight line trajectories (Fig. 3(a)). When a longitudinal magnetic field is added electrons start to revolve around the bubble as a result of the magnetic force, this force combined with the electric force induced by the bubble completely modifies the dynamics of the electrons. The gyro-radius of the electrons with $p_y \neq 0$ is reduced when B_0 is raised. Therefore the corresponding flight path in the (x, y) plane appear to be bent, the trajectory will be even more curved when the

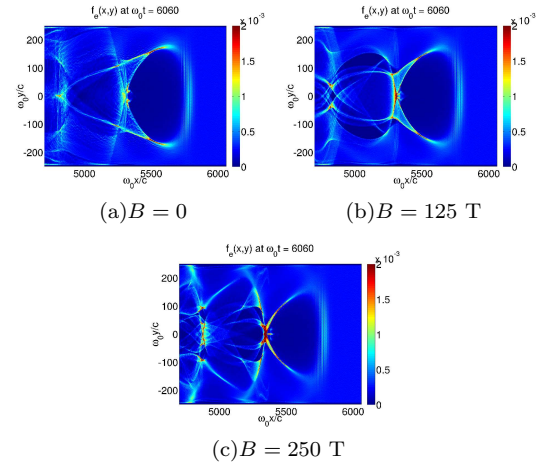


FIG. 3: Electron density long after the collision of the two waves. P linear polarizations. $a = 4$, $a_1 = 0.1$ and $n_e = 2.5 \times 10^{-4} n_c$.

applied field is stronger (Figs. 3(b)-3(c)). When electrons revolve around the bubble they create a current perpendicularly to the plane of the figure, as evidenced by Figs. 4(a)-4(b). Given the value of the electronic density at the rear of the bubble ($1 \times 10^{-3} \leq n_e \leq 1.5 \times 10^{-3}$), we deduce from Figs. 4 the time averaged speed v_z^{avg} of electrons revolving around the bottleneck of the bubble $0.5 \leq v_z^{\text{avg}}/c \leq 0.8$. This current will act as a small solenoid, and thus the longitudinal magnetic field will be amplified. This feature and its influence on the beam dynamics will be detailed in the next subsection.

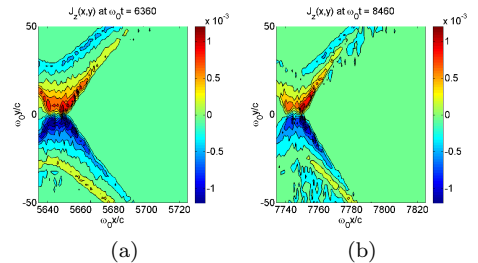


FIG. 4: Transverse component of the current density (normalized by $en_c c$), the wakefield propagates in a magnetized plasma ($B = 250 \text{T}$). $a = 4$, $a_1 = 0.1$ and $n_e = 2.5 \times 10^{-4} n_c$.

B. A new mechanism to enhance the beam quality

The intensity of the magnetic field is almost doubled locally (Figs. 5) compared to the initial ($t = 0$) uniform map of B_x . We shall underline that this pattern is stable as we obtain quasi identical maps of B_x in this region of the bubble when the pump pulse has just entered the

plasma around $\omega_0 t = 2280$. Moreover we note that the geometry of the magnetic field lines is weakly altered by the electronic density modulations induced by the propagating bubble. Magnetic field lines stay almost parallel to the propagation direction. Let us now examine the

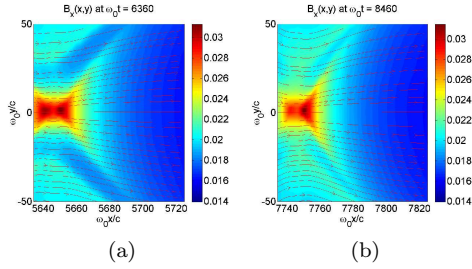


FIG. 5: Longitudinal component of the magnetic field (normalized by $m_e \omega_0 / e$), the wakefield propagates in a magnetized plasma $B_0 = 250$ T (*i.e.* $\bar{B}_0 \sim 18.7 \times 10^{-3}$). $a = 4$, $a_1 = 0.1$ and $n_e = 2.5 \times 10^{-4} n_c$. Magnetic field lines are superimposed (red curves) on B_x colormap.

effect of the magnetic field on the dynamics of the accelerated beam. To evidence the differences between the magnetized and the unmagnetized regimes, we plotted kinetic energy density maps showing the evolution of the trapped beam at the rear of the bubble. In the unmagnetized case (Figs. 6), the beam alternatively explodes (due to space charge effects) and focalises (due to the focalizing effect of the transverse electric field). This behavior has a typical $\sim 2000 \omega_0^{-1}$ period. Note that the beam acceleration is degraded because the components of the splitted beam will not see the maximal value of the longitudinal electric field (which is located on axis). The dynamics is completely different in the magnetized case (Figs. 7), the longitudinal magnetic field is strong enough to curve the trajectories and hinder the explosion of the beam. As a result the beam is almost concentrated on axis, the transverse emittance is reduced and the main part of the beam, which also corresponds to the region where the magnetic field is the strongest, always sees the maximum value of the electric field. Next we will quantify the enhancement of the beam quality through the evolution of the energy distribution functions of the beam.

C. Enhancement of the beam quality

As already mentionned, in the magnetized case, the beam is submitted to a more uniform accelerating field, this pattern boosts the particle acceleration leading to a slightly higher maximum kinetic energy when compared to the unmagnetized case (Fig. 8).

The focalizing magnetic field reduces the low energy tail of the energy spectrum, as can be seen in Figs 8. Obviously, this trend is enhanced when the guide field rises. With no guide field, the relative variation

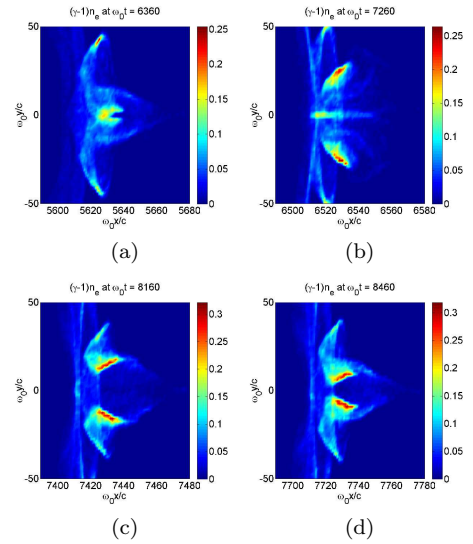


FIG. 6: Electron kinetic energy density (normalized by $m_e c^2 n_c$), the wakefield propagates in a non magnetized plasma ($B_0 = 0$). $a = 4$, $a_1 = 0.1$ and $n_e = 2.5 \times 10^{-4} n_c$.

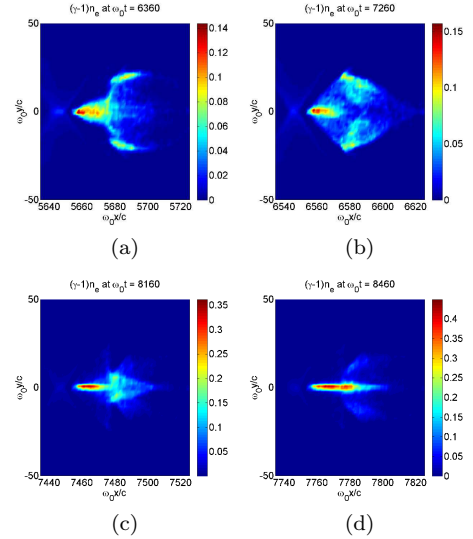


FIG. 7: Electron kinetic energy density (normalized by $m_e c^2 n_c$), the wakefield propagates in a magnetized plasma ($B_0 = 250$ T). $a = 4$, $a_1 = 0.1$ and $n_e = 2.5 \times 10^{-4} n_c$.

of the energy at full width at half maximum (fwhm) $\Delta E_{fwhm}/E_{max} \approx 1\%$ is excellent, but the rms value of the energy spread has small variations and reaches 7% at the end of the simulation (Table I). When $B_0 = 125$ T, on the one hand the spread of the low energy tail of the distribution is reduced as shown by Fig. 8(a), and confirmed by the rms value $\sim 4\%$, but on the other hand $\Delta E_{fwhm}/E_{max}$ is slightly degraded. When $B_0 = 250$ T, untrapped electrons carrying energies about 10 MeV concentrate (n_e locally reaches $1.5 \times 10^{-3} n_c$) at the rear of

$\omega_0 t$	7000	9000	11000	13000
B_0 (T)				
0	5.33% (2.05%)	5.88% (1.09%)	4.53% (0.81%)	6.61% (0.97%)
125	5.50% (5.03%)	5.45% (4.89%)	3.41% (1.94%)	3.96% (1.58%)
250	3.96% (3.72%)	2.67% (2.75%)	2.84% (1.54%)	2.91% (0.63%)

TABLE I: Evolution of the half width of the electron distribution function with $a = 4$, $a_1 = 0.1$, $n_e = 2.5 \times 10^{-4}$. Standard deviation, *i.e.* rms value, and relative variation ($\Delta E_{fwhm}/E_{max}$) of the distribution, where the subscript *fwhm* denotes the Full Width at Half Maximum.

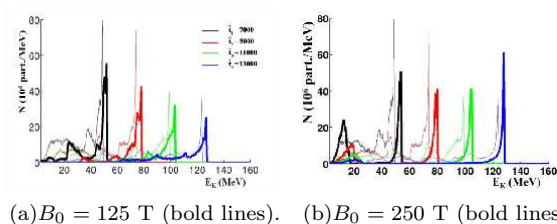


FIG. 8: Electron energy distribution from 2D PIC simulations. P linear polarizations. $a = 4$, $a_1 = 0.1$ and $n_e = 2.5 \times 10^{-4} n_c$. Dashed lines correspond to $B = 0$.

the bubble. These low energy (*i.e.* $0 < E_K < 25$ MeV) electrons are evidenced by bumps in the beam energy distribution (Fig 8(b)). This low energy bump slowly slides out of the simulation box as these electrons are not injected in the wakefield, and therefore should not be considered for the interpretation of the diagnostics concerning the accelerated beam. According to this comment, we note that a 250 T guide field is enough to completely suppress the low energy tail during the whole simulation. A clear enhancement of the beam quality is obtained, first the final rms value is below 3% and $\Delta E_{fwhm}/E_{max} < 1\%$ (table I) thus providing a very sharp control on the final energy of the beam, and second the number of electrons at the highest energies does not vanish, as in the unmagnetized case, but on the contrary grows up to 60×10^6 part/MeV, nearly twice the value of the unmagnetized case ! To our knowledge such an acute mono-energetic electron beam production, with complete extinction of the low energy tail has never been evidenced.

For a given pump pulse, two well-known controllers of the low intensity laser can be used to optimize the beam quality. The low intensity pulse duration can be monitored and the transverse fwhm of the spatial envelope adjusted, these two parameters together usually make it possible to get a quasi-mono-energetic electron beam in the blow-out regime [14, 25]. There are other ways to enhance the beam quality. For example, one can resort to a

longitudinal gradient of the electronic density to enhance trapping [14, 31, 32]. In an alternate approach, assuming initially homogenous plasma, one can slowly evolve the laser pulse shape to alternate periods of expansion and contraction of the bubble, to respectively trigger and stop self-injection [33] of the electrons into the bubble. However this technique seems hard to adjust to get a unique mono-energetic bunch. In this paper, injected electrons are confined by using a magnetic guide field but we note that the intensity of the field, required to substantially enhance the beam quality, depends on lasers pulse shapes and durations. In this section we did not pay attention to the tuning of the low intensity colliding pulse, we have shown that the guiding induced by B_0 is enough beyond some threshold, function of the parameters of the simulation. However, if we decide to lower the blowout stability by increasing the main pulse intensity, the required intensity of the guide field grows to values largely out of reach of the current technology, then fine-tuning of the colliding pulse becomes necessary. The next section is devoted to this issue.

IV. INFLUENCE OF A MAGNETIC GUIDE FIELD AT HIGHER INTENSITIES

A very high intensity wave is considered now, the pump pulse which is linearly polarized is assumed to have a peak normalized intensity $a = 10$, and a duration of 30 fs. It is focused to a $35.65 \mu\text{m}$ large focal spot. The colliding pulse has a peak normalized intensity $a_1 = 0.1$, a 30fs duration and three focal spot sizes were considered $D = 60 \mu\text{m}$, $36 \mu\text{m}$ and $10 \mu\text{m}$. The wavelength of the waves is $\lambda = 0.8 \mu\text{m}$. In these simulations, the plasma density is still $n_e = 2.5 \times 10^{-4} n_c$. Unless otherwise mentioned the following simulations were run with $B_0 = 125\text{T}$. When considering $a = 10$ and a counter-propagating wave focused to a $10 \mu\text{m}$ focal spot, one has a paramount effect of the magnetic field on the distribution function (Table II, Fig. 9). The electron energy distribution becomes almost mono-energetic. After the laser pulse has propagated through the plasma by 3.8 mm, the electron energy distribution is still quite mono-kinetic and the maximum electronic energy exceeds one GeV (Fig. 9(b)). Table II shows the evolution of the energy spread of the electron energy distribution with time. When no field is applied the quality decreases whereas we get an acute control on the beam energy with B_0 . It must be pointed out that the accelerated charge is small (close to 50 picocoulombs). The electron energy distributions corresponding to four focal spots are compared at some time. Figure 13 shows that the distribution becomes much more mono-energetic when the focal spot of the perturbing wave is smaller than the one of the main pulse. The magnetic field is much more efficient when considering a small value of D . Then, we have checked that this peak exists in a very small range of values close to $a_1 = 0.1$. When $a_1 = 0.08$ the distribution function

$\omega_0 t$	7000	13000	22000	30000
B_0 (T)				
0	40.5% (23.0%)	41.2% (86.1%)	36.0% (59.3%)	33.2% (100.9%)
125	6.4% (4.85%)	1.7% (1.3%)	5.0% (2.0%)	3.35% (2.6%)

TABLE II: Evolution of the half width of the electron distribution function. $a = 10$, $a_1 = 0.1$, $n_e = 2.5 \times 10^{-4}$. Standard deviation, *i.e.* rms value, and relative variation ($\Delta E_{fwhm}/E_{max}$) of the distribution.

shows a lower magnitude peak, and the charge accelerated in the first bubble is about 10 picocoulombs. The peak still exists when $a_1 = 0.102$. But in the case of a higher value of a_1 (for instance $a_1 = 0.15$) the energy distribution does not show a very thin high-energy peak any longer because the injected charge is higher and the magnetic field is too weak to concentrate the beam efficiently.

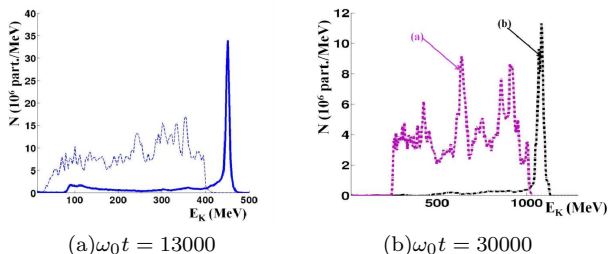


FIG. 9: Electron energy distribution from 2D PIC simulations with $a = 10$, $a_1 = 0.1$, $n_e = 2.5 \times 10^{-4} n_c$ and $D = 10 \mu\text{m}$. The dashed line corresponds to $B_0 = 0$ and the bold one to $B_0 = 125$ T.

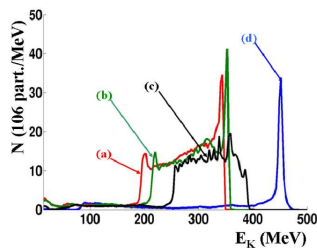


FIG. 10: Electron energy distribution from 2D PIC simulations at $\omega_0 t = 13000$ with $a = 10$, $a_1 = 0.1$, $n_e = 2.5 \times 10^{-4} n_c$ and $B_0 = 125$ T. (a) $D = 59.5 \mu\text{m}$, (b) $D = 35.7 \mu\text{m}$, (c) $D = 20 \mu\text{m}$, (d) $D = 10 \mu\text{m}$.

No high-energy peak was seen in the distribution function for larger values of a_1 , actually the same kind of distribution is obtained when $a_1 = 0.2$, $a_1 = 0.5$ and $a_1 = 1$. Figure 11 shows that the electron energy distribution becomes more mono-energetic when the mag-

nitude of the magnetic guide field is increased to 250 T, accordingly with the results obtained with a lower intensity of the pump pulse ($a_0 = 4$) in section III C. Figure 12 shows that, a shorter pulse duration ($\Delta t = 10$ fs) for the counterpropagating wave, also makes the electron energy distribution more mono-energetic. Then, in order to obtain a more mono-energetic distribution when $a = 10$ and $a_1 = 1$, a very strong magnetic field $B_0 = 250$ T and a short duration for the counterpropagating wave $\Delta t = 10$ fs were considered (Fig. 13). As expected, a high energy peak is obtained. One should point out that the charge accelerated in the first bubble is still close to 50 picocoulombs. To summarize when a_1 is too high, that is when the charge injected in the wakefield exceeds some threshold, we can not stop a drop of the beam quality by imposing an external field alone, at least the main parameters (focal spot size and duration) of the colliding pulse shall be reduced.

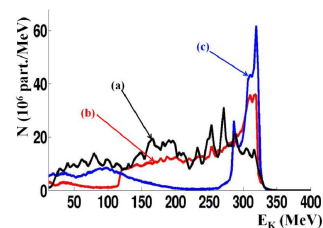


FIG. 11: Electron energy distribution from 2D PIC simulations at $\omega_0 t = 13000$ with $a = 10$, $a_1 = 1$, $n_e = 2.5 \times 10^{-4} n_c$, $D = 10 \mu\text{m}$ and $\Delta t = 30$ fs. (a) $B_0 = 0$, (b) $B_0 = 125$ T, (c) $B_0 = 250$ T.

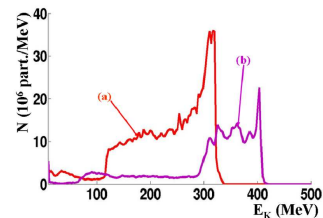


FIG. 12: Electron energy distribution from 2D PIC simulations at $\omega_0 t = 13000$ with $a = 10$, $a_1 = 1$, $n_e = 2.5 \times 10^{-4} n_c$, $B_0 = 125$ T and $D = 10 \mu\text{m}$. (a) $\Delta t = 30$ fs, (b) $\Delta t = 10$ fs.

V. CONCLUSIONS

In the first part of this paper, we summarized some essential results about the most efficient choice of polarizations for injection in the bubble, in the colliding pulse scheme. At rather high electron density ($\gtrsim 10^{-3} n_c$) and moderately relativistic electromagnetic wave intensity ($a_0 \lesssim 2$), more particles are accelerated to high energies in the case of P linear polarizations that is

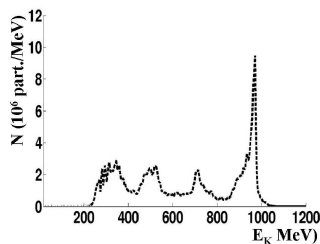


FIG. 13: Electron energy distribution from 2D PIC simulations at $\omega_0 t = 30000$ with $a = 10$, $a_1 = 1$, $n_e = 2.5 \times 10^{-4} n_c$ and $B_0 = 250$ T. The spatio-temporal shape of the laser envelope is defined by $D = 10 \mu\text{m}$ and $\Delta t = 10\text{fs}$.

to say when electrons undergo the action of the beat-wave force and all the others. For higher intensities and lower densities ($\sim 10^{-4} n_c$) the beatwave force, that is cold injection, can be more efficient. The second and main part of this paper has been devoted to the study of the influence of an external static magnetic field on the wakefield acceleration process, within the colliding pulse scheme. To our knowledge this idea was never explored. The magnetic field is supposed parallel to the

direction of propagation of the two counter-propagating waves. It has been shown that the B_0 field creates a transverse current, the latter current can induce a raise of B_x at the rear bottleneck of the bubble. Therefore the beam dynamics is substantially modified as the beam is constrained to stay in the maximum acceleration region of the bubble. Beam emittance is considerably reduced and maximum kinetic energy slightly boosted compared to the unmagnetized case. This mechanism provides means to dramatically enhance the beam quality in the blowout regime. We achieved tremendous amelioration with the setup: $a = 10$, $a_1 = 0.1$ and $n_e = 2.5 \times 10^{-4} n_c$. After roughly 4 mm of wakefield acceleration, without B_0 field the electronic energy distribution is noisy $\Delta E_{fwhm}/E_{max} \sim 100\%$ whereas we get $\Delta E_{fwhm}/E_{max} \lesssim 3\%$ when the plasma is magnetized with a 125 T field. Nevertheless the intensity of the B_0 field may be limited by technological considerations [30], thus acute control of the beam quality may require some fine-tuning of the colliding pulse parameters. For a given pump pulse, one should adapt the intensity, duration and focal spot size of the counter-propagating laser pulse.

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